

# DBQ: A Differentiable Branch Quantizer for Lightweight Deep Neural Networks

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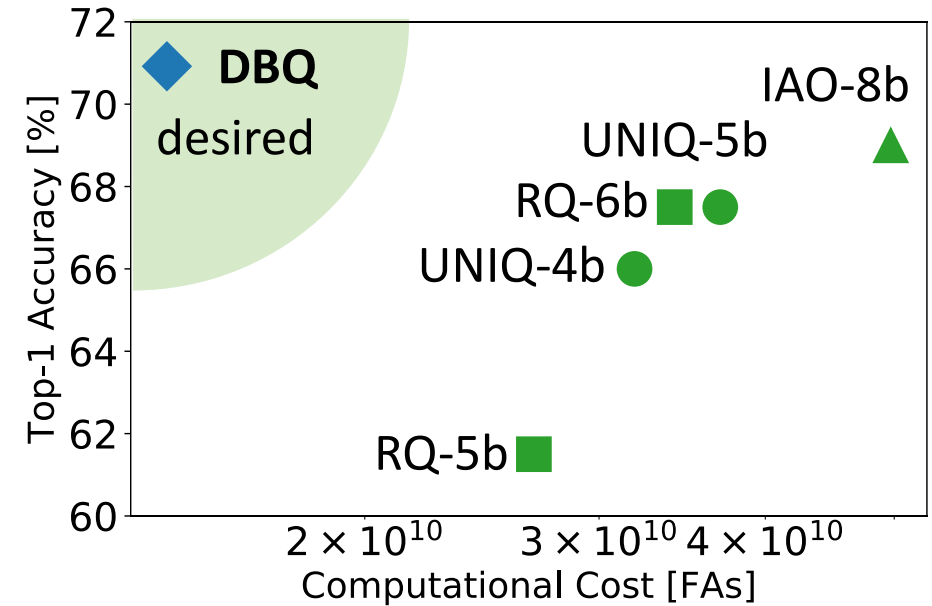
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# Motivation

- The complexity of DNNs inhibits their deployment on resource-constrained devices
- Current quantization methods offer *conservative* complexity reduction for *lightweight* networks:
- A ternarized MobileNetV1 incurs a massive (6%) accuracy drop



**Goal:** aggressively quantize lightweight networks while maintaining accuracy

# Ternary Branch Quantization

- Quantizing parameters to two ternary branches:
  - utilizes efficient ternary arithmetic
  - offers a 9-level non-uniform quantizer
- How to train networks with such a structure **efficiently**?

regular computation

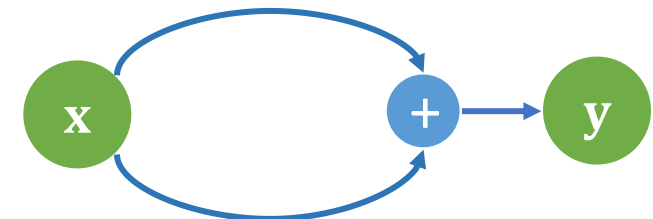


quantize  $w$



ternary branch computation

$$w_1 \in \{-\alpha_1, 0, \alpha_1\}$$



$$w_2 \in \{-\alpha_2, 0, \alpha_2\}$$

# Differentiable Branch Quantizer (DBQ)

- Formulate a  $B$ -branch ternary quantizer as a non-uniform quantizer with  $N = 3^B$  levels:

$$Q(\mathbf{w}) = \gamma_2 \left[ \sum_{i=1}^{N-1} \left[ f(\gamma_1 \mathbf{w} - t_i) \sum_{j=1}^B b_{i,j} \alpha_j \right] - \sum_{j=1}^B \alpha_j \right]$$

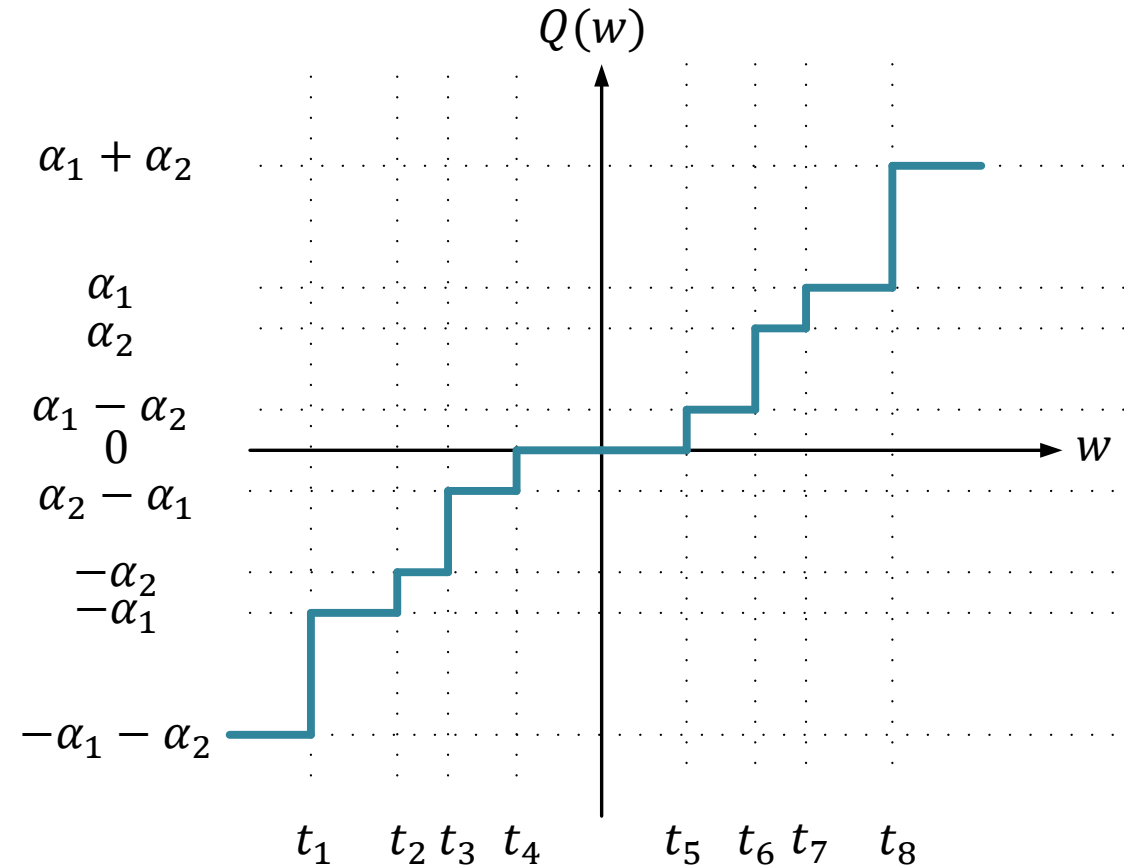
Where:

- $f$  is an ideal step function
  - $\{\alpha_j\}_{j=1}^B$  are the branch scales
  - $\{t_i\}_{i=1}^{N-1}$  are the quantizer thresholds
  - $\gamma_1$  &  $\gamma_2$  are pre/post quantization scales
- The ternary structure is enforced by the choice of  $b_{i,j}$ 's

# Example: Two Ternary Branches

- A two-ternary branch quantizer can be written as:

$$\begin{aligned}
 Q(\mathbf{w}) = & \gamma_2 \left[ \alpha_2 f(\gamma_1 \mathbf{w} - t_1) + (\alpha_1 - \alpha_2) f(\gamma_1 \mathbf{w} - t_2) \right. \\
 & + (2\alpha_2 - \alpha_1) f(\gamma_1 \mathbf{w} - t_3) + (\alpha_1 - \alpha_2) f(\gamma_1 \mathbf{w} - t_4) \\
 & + (\alpha_1 - \alpha_2) f(\gamma_1 \mathbf{w} - t_5) + (2\alpha_2 - \alpha_1) f(\gamma_1 \mathbf{w} - t_6) \\
 & + (\alpha_1 - \alpha_2) f(\gamma_1 \mathbf{w} - t_7) + \alpha_2 f(\gamma_1 \mathbf{w} - t_8) \\
 & \left. - (\alpha_1 + \alpha_2) \right]
 \end{aligned}$$



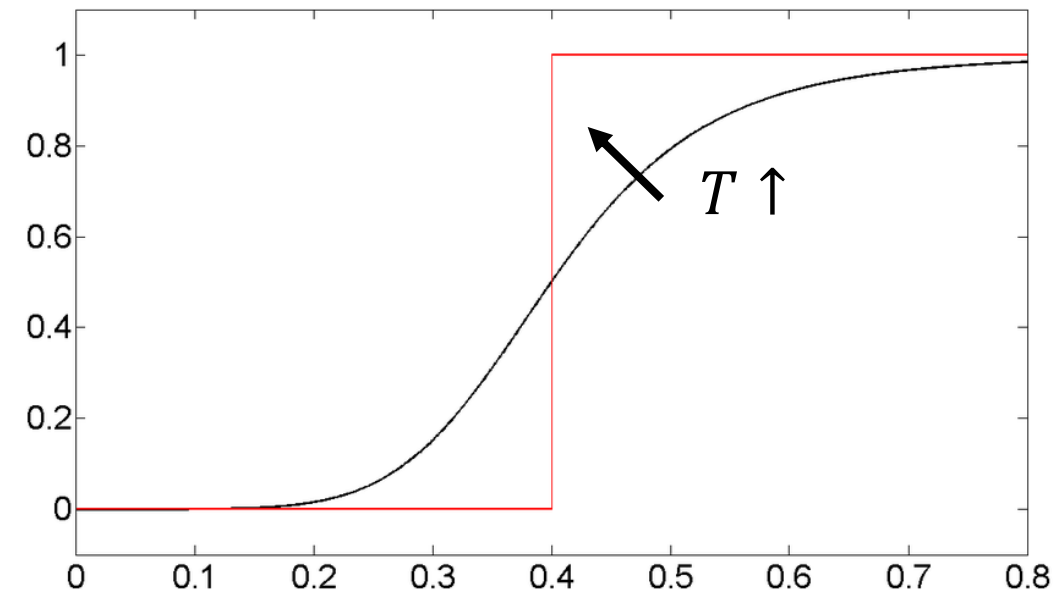
# Differentiability in DBQ

- The non-differentiability of the quantizer comes from the step function  $f()$
- **Solution:** use an approximate smooth function  $\hat{f}_T()$  (e.g. Sigmoid) with a temperature parameter  $T$  that controls the approximation error:

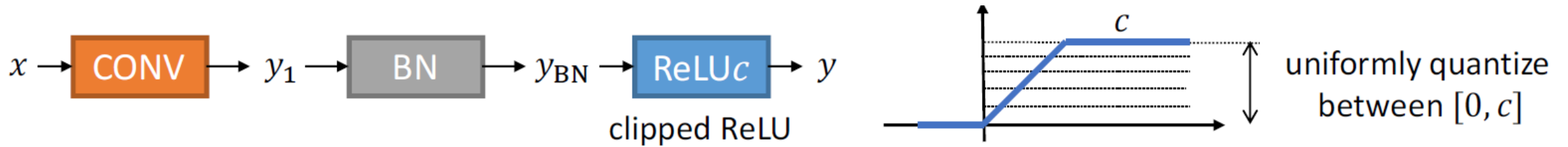
$$e_T(u) = \hat{f}_T(u) - f(u) \xrightarrow{T \rightarrow \infty} 0$$

$f()$ : step function

$\hat{f}_T()$ : temperature controlled Sigmoid



# Activation Quantization



- Quantizing activations requires an appropriate clipping value  $c$
- Leverage activation statistics offered by BatchNorm (BN) layers to choose  $c$ :

$$c = \max_{i \in [C]} \beta_i + k\gamma_i$$

$\beta_i$  and  $\gamma_i$ : the per-channel BN shift and scale parameters;  $k$  controls clipping probability

# Complexity Metrics

- **Computational Cost ( $\mathcal{C}_C$ ):** captures the number of 1-b full adders (FA) needed to implement the dot-products required for a single inference
- **Sparsity-Aware Computational Cost ( $\mathcal{C}_S$ ):** analogous to  $\mathcal{C}_C$ , defined in order to leverage weight-sparsity in different models that can be reflected on the model complexity
- **Representational Cost ( $\mathcal{C}_R$ ):** measures the number of bits needed to represent the entire network (both weights and activations) for a single inference
- **Model Storage Cost ( $\mathcal{C}_M$ ):** analogous to  $\mathcal{C}_R$ , but only accounts for the weight storage as it is useful for studying model compression



# CIFAR10 Results: ResNet-20

Compared to a binary branch quantizer for ResNet-20:

- DBQ achieves **higher** accuracy with **lower** complexity at iso-number of branches (by exploiting **weight sparsity**)
- DBQ-2T achieves a 56% reduction in  $\mathcal{C}_S$ , at **iso-accuracy**

Method	Acc. ( $\Delta$ ) [%]	$\mathcal{C}_C$ ( $\mathcal{C}_S$ ) [ $10^9$ FA]	$\mathcal{C}_R$ ( $\mathcal{C}_M$ ) [ $10^6$ b]
FP [30]	92.10 (/)	23.73 (23.73)	14.63 (8.63)
LQNet-1B [30]	90.10 (-2.171)	1.60 (1.60)	6.34 (0.35)
LQNet-2B [30]	91.80 (-0.325)	2.83 (2.83)	6.61 (0.61)
LQNet-3B [30]	92.00 (-0.108)	4.07 (4.07)	6.88 (0.88)
FP (Ours)	92.00 (/)	23.73 (23.73)	14.63 (8.63)
DBQ-1T (Ours)	<b>91.06 (-1.021)</b>	<b>1.60 (0.92)</b>	6.61 (0.61)
DBQ-2T (Ours)	<b>91.93 (-0.076)</b>	<b>2.83 (1.79)</b>	7.15 (1.15)





# Ablation Study: MobileNetV1 on ImageNet

- **DBQ-1T** (one ternary branch) achieves a massive reduction in  $\mathcal{C}_C$  compared to FP but at a **catastrophic** loss of 5.67% in accuracy
- **DBQ-2T-1** (two ternary branches) recovers the accuracy to within 1.03% of FP while also achieving **massive** savings in  $\mathcal{C}_C$  of 84%

Model Name	Activations	FL	DW	PW	FC	Top-1/5 Acc. [%]	$\mathcal{C}_C$ ( $\mathcal{C}_S$ ) [ $10^{10}$ FA]	$\mathcal{C}_R$ ( $\mathcal{C}_M$ ) [ $10^7$ b]
FP	ReLU - 32b	32b	32b	32b	32b	<b>72.12/90.43</b>	33.37 (33.37)	30.00 (13.54)
FX8-1	ReLU6 - 8b	32b	8b	8b	32b	71.65/90.17	5.78 (5.39)	10.38 (5.90)
FX8-2	ReLU6 - 8b	8b	8b	8b	8b	71.60/90.19	5.24 (4.85)	7.56 (3.44)
FX8-3	ReLU $x$ - 8b	8b	8b	8b	8b	<b>71.86/90.26</b>	5.24 (4.85)	7.56 (3.44)
→ DBQ-1T	ReLU - 32b	32b	32b	1T	32b	66.45/86.72	3.60 (2.61)	20.58 (4.12)
→ DBQ-2T-1	ReLU - 32b	32b	32b	2T	32b	71.09/89.71	5.23 (3.77)	21.21 (4.75)
DBQ-2T-2	ReLU6 - 8b	32b	8b	2T	32b	70.25/89.42	2.73 (1.97)	9.12 (4.64)
DBQ-2T-3	ReLU $x$ - 8b	32b	8b	2T	32b	70.80/89.75	2.73 (1.97)	9.12 (4.64)
DBQ-2T-4	ReLU $x$ - 8b	8b	8b	2T	8b	<b>70.92/89.61</b>	<b>2.18 (1.42)</b>	<b>6.30 (2.18)</b>

# Ablation Study: MobileNetV1 on ImageNet

- The Top-1 accuracy of **FX8-3** (BN-based clipping) is better than **FX8-2** (ReLU6-based clipping) without any overhead in training or inference
- Similarly for **DBQ-2T-3** and **DBQ-2T-2**

Model Name	Activations	FL	DW	PW	FC	Top-1/5 Acc. [%]	$\mathcal{C}_C$ ( $\mathcal{C}_S$ ) [ $10^{10}$ FA]	$\mathcal{C}_R$ ( $\mathcal{C}_M$ ) [ $10^7$ b]
FP	ReLU - 32b	32b	32b	32b	32b	<b>72.12/90.43</b>	33.37 (33.37)	30.00 (13.54)
FX8-1	ReLU6 - 8b	32b	8b	8b	32b	71.65/90.17	5.78 (5.39)	10.38 (5.90)
 FX8-2	ReLU6 - 8b	8b	8b	8b	8b	71.60/90.19	5.24 (4.85)	7.56 (3.44)
 FX8-3	ReLU $_x$ - 8b	8b	8b	8b	8b	<b>71.86/90.26</b>	5.24 (4.85)	7.56 (3.44)
DBQ-1T	ReLU - 32b	32b	32b	1T	32b	66.45/86.72	3.60 (2.61)	20.58 (4.12)
DBQ-2T-1	ReLU - 32b	32b	32b	2T	32b	71.09/89.71	5.23 (3.77)	21.21 (4.75)
 DBQ-2T-2	ReLU6 - 8b	32b	8b	2T	32b	70.25/89.42	2.73 (1.97)	9.12 (4.64)
 DBQ-2T-3	ReLU $_x$ - 8b	32b	8b	2T	32b	70.80/89.75	2.73 (1.97)	9.12 (4.64)
DBQ-2T-4	ReLU $_x$ - 8b	8b	8b	2T	8b	<b>70.92/89.61</b>	<b>2.18 (1.42)</b>	<b>6.30 (2.18)</b>

# Ablation Study: MobileNetV1 on ImageNet

- **DBQ-2T-4**, which is **DBQ-2T-1** with the remaining layers quantized to 8b, incurs a **minimal loss** in accuracy (1.2%) compared to FP while also achieving even **greater reduction** in both  $\mathcal{C}_C$  (93%) and  $\mathcal{C}_R$  (70%). The reduction in  $\mathcal{C}_S$  increases to 96% when **branch sparsity is exploited** to skip computations.

Model Name	Activations	FL	DW	PW	FC	Top-1/5 Acc. [%]	$\mathcal{C}_C$ ( $\mathcal{C}_S$ ) [ $10^{10}$ FA]	$\mathcal{C}_R$ ( $\mathcal{C}_M$ ) [ $10^7$ b]
FP	ReLU - 32b	32b	32b	32b	32b	<b>72.12/90.43</b>	33.37 (33.37)	30.00 (13.54)
FX8-1	ReLU6 - 8b	32b	8b	8b	32b	71.65/90.17	5.78 (5.39)	10.38 (5.90)
FX8-2	ReLU6 - 8b	8b	8b	8b	8b	71.60/90.19	5.24 (4.85)	7.56 (3.44)
FX8-3	ReLU $x$ - 8b	8b	8b	8b	8b	<b>71.86/90.26</b>	5.24 (4.85)	7.56 (3.44)
DBQ-1T	ReLU - 32b	32b	32b	1T	32b	66.45/86.72	3.60 (2.61)	20.58 (4.12)
→ DBQ-2T-1	ReLU - 32b	32b	32b	2T	32b	71.09/89.71	5.23 (3.77)	21.21 (4.75)
DBQ-2T-2	ReLU6 - 8b	32b	8b	2T	32b	70.25/89.42	2.73 (1.97)	9.12 (4.64)
DBQ-2T-3	ReLU $x$ - 8b	32b	8b	2T	32b	70.80/89.75	2.73 (1.97)	9.12 (4.64)
→ DBQ-2T-4	ReLU $x$ - 8b	8b	8b	2T	8b	<b>70.92/89.61</b>	<b>2.18 (1.42)</b>	<b>6.30 (2.18)</b>

# ImageNet Results: MobileNetV1

- DBQ-2T achieves the **lowest** computational cost compared to previously published works, while achieving the **highest** Top-1 accuracy 70.92%

Method	Act.	FL	DW	PW	FC	Top-1 Acc. [%]	$\mathcal{C}_C (\mathcal{C}_S)$ [ $10^{10}$ FA]	$\mathcal{C}_R (\mathcal{C}_M)$ [ $10^7$ b]
IAO* [12]	8b	8b	8b	8b	8b	<b>69.00*</b>	4.97 (/)	7.49 (3.37)
UNIQ [1]	8b	5b	5b	5b	5b	67.50	3.70 (/)	6.29 (2.18)
UNIQ [1]	8b	4b	4b	4b	4b	66.00	3.19 (/)	5.87 ( <b>1.76</b> )
UNIQ [1]	8b	8b	8b	8b	8b	68.25	5.24 (/)	7.56 (3.44)
QSM* [27]	8b	8b	8b	8b	8b	68.03	4.97 (/)	7.49 (3.37)
RQ [19]	5b	5b	5b	5b	5b	61.50	<b>2.68</b> (/)	<b>4.75</b> (2.18)
RQ [19]	6b	6b	6b	6b	6b	67.50	3.42 (/)	5.69 (2.60)
HAQ cloud [28]	mixed	8b	mixed	mixed	8b	65.33 – 71.20 <sup>†</sup>	2.73 (/)	5.09 (3.12)
HAQ edge [28]	mixed	8b	mixed	mixed	8b	67.40 – 71.20 <sup>†</sup>	4.06 (/)	5.87 (2.49)
FP (Ours)	32b	32b	32b	32b	32b	<b>72.12</b>	33.37 (33.37)	30.00 (13.54)
FX8 (Ours)	8b	8b	8b	8b	8b	<b>71.86</b>	5.24 (4.85)	7.56 (3.44)
DBQ-2T (Ours)	8b	8b	8b	2T	8b	<b>70.92</b>	<b>2.18 (1.42)</b>	6.30 (2.18)

\*models with BN folding

\*results extracted from a plot

<sup>†</sup>exact accuracy not reported

# ImageNet Results: MobileNetV2 & ShuffleNetV2

- Inline with our experiments on MobileNetV1, we quantize all PW layers using 2T, with the remaining layers and activations quantized to 8b fixed-point.
- Observe a **minimal** 1.3% (MobileNetV2) and 2.6% (ShuffleNetV2) drop in accuracy compared to FP, while achieving **massive** (77% - 95%) reductions in all the complexity metrics.

Model	Act.	FL	DW	PW	FC	Top-1 Acc. [%]	$\mathcal{C}_C$ ( $\mathcal{C}_S$ ) [ $10^{10}$ FA]	$\mathcal{C}_R$ ( $\mathcal{C}_M$ ) [ $10^7$ b]
MobileNetV2-FP	32b	32b	32b	32b	32b	71.88	17.83 (17.83)	32.87 (11.22)
MobileNetV2-2T	8b	8b	8b	2T	8b	<b>70.54</b>	<b>1.42 (1.11)</b>	<b>7.45 (2.04)</b>
ShuffleNetV2-FP	32b	32b	32b	32b	32b	69.36	8.52 (8.52)	13.81 (7.29)
ShuffleNetV2-2T	8b	8b	8b	2T	8b	<b>66.74</b>	<b>0.64 (0.46)</b>	<b>3.21 (1.38)</b>

# Accuracy-Precision-Complexity Trade-off: Dataset

[Chowdhery, arXiv'19]

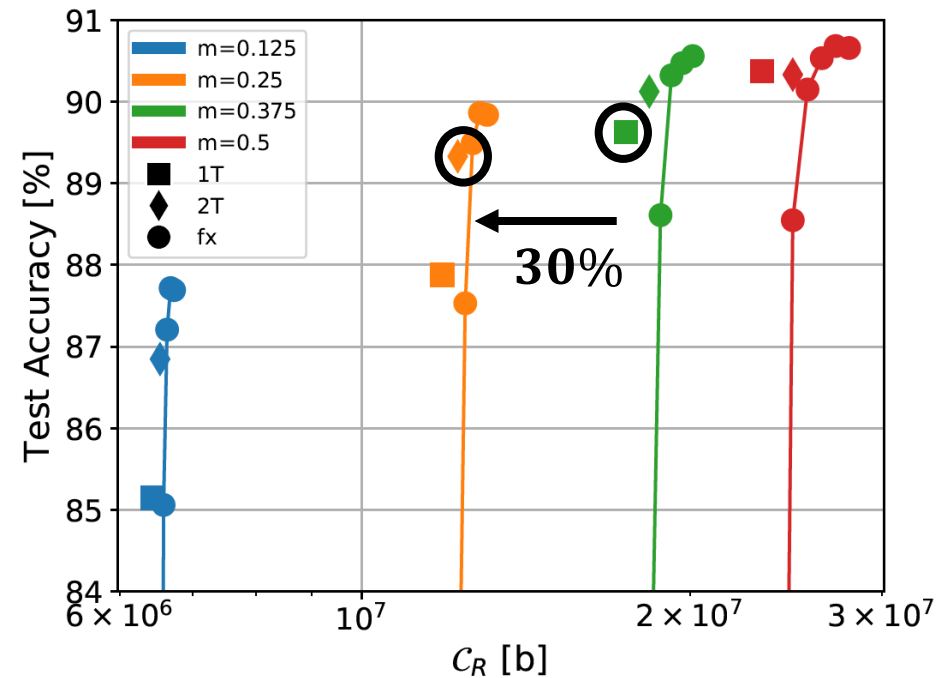
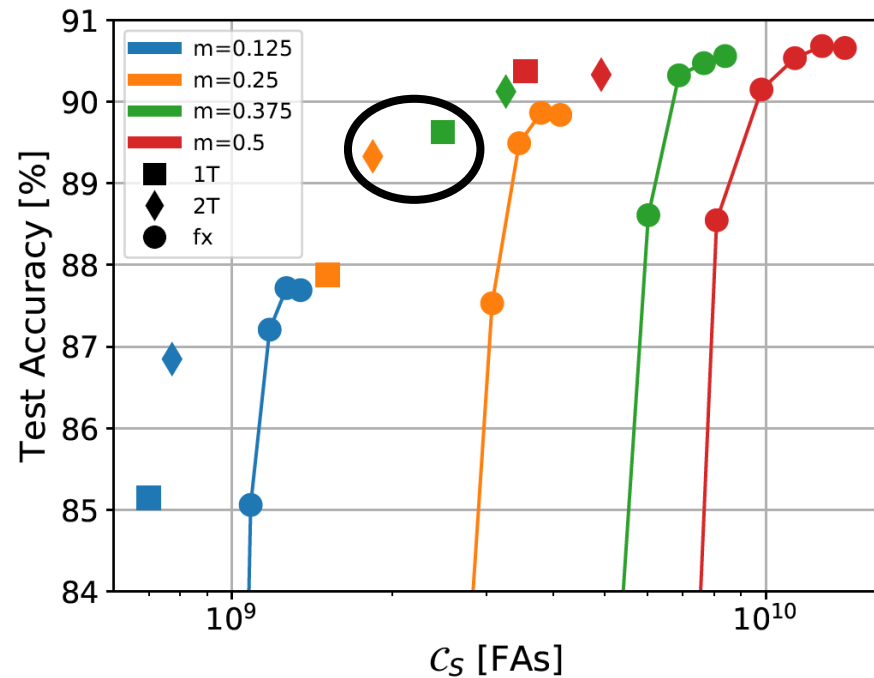
## Google's Visual Wake Words (VWW) Dataset:

- Binary classification problem (person, no-person)
- Images taken from COCO'14 dataset
- Contains 115k training images and 8k validation images
- Reflects a real-life detection scenario for always-on resource-constrained Edge devices



# Accuracy-Precision-Complexity Trade-off: Results

- MobileNetV1 complexity is varied via the width multiplier  $m$  which controls the number of channels
- DBQ models form a **pareto-optimal curve**
- For **lightweight models**: going from 1T to 2T is better than increasing  $m$





# Thank You!

paper link:

<https://arxiv.org/abs/2007.09818>